

Determine the convergence or divergence of the series and identify the test that was used.

1. $\sum_{n=0}^{\infty} \frac{n!}{3^n}$

2. $\sum_{n=1}^{\infty} n \left(\frac{3}{4} \right)^n$

3. $\sum_{n=1}^{\infty} \frac{2^n}{n^2}$

4. $\sum_{n=1}^{\infty} \frac{n!}{n3^n}$

5.
$$\sum_{n=0}^{\infty} \frac{3^n}{(n+1)^n}$$

6.
$$\sum_{n=2}^{\infty} \left(\frac{2n+1}{n-1} \right)^n$$

$$7. \sum_{n=1}^{\infty} (2\sqrt{n} + 1)^n$$

$$8. \sum_{n=1}^{\infty} \left(\frac{1}{n} - \frac{1}{n^2} \right)^n$$

9. $\sum_{n=1}^{\infty} \frac{3}{n\sqrt{n}}$

10. $\sum_{n=1}^{\infty} \frac{(-1)^n 3^{n-2}}{2^n}$

$$11. \sum_{n=1}^{\infty} \frac{\cos n}{2^n}$$

$$12. \sum_{n=1}^{\infty} \frac{(-1)^n 3^{n-1}}{n!}$$

$$13. \sum_{n=1}^{\infty} (-1)^n \frac{(n!)^2}{(3n)!}$$

$$14. \sum_{n=1}^{\infty} (-1)^n \frac{e^{n^2}}{n^n}$$

$$15. \sum_{n=2}^{\infty} (-1)^n \frac{1}{n \ln n}$$

$$16. \sum_{n=1}^{\infty} \frac{3^n n!}{(2n)!}$$

17. Find the interval of convergence of the following power series.

a.
$$\sum_{n=0}^{\infty} \frac{(-1)^{n+1} (x-1)^{n+1}}{n+1}$$

b. $\sum_{n=1}^{\infty} \frac{n}{n+1} (-2x)^{n-1}$